

**YOU EITHER DO IT OR YOU DO IT 2023**

- Factorize  $x^4 + x^2y^2 + y^4$  completely. (04 marks)
- Solve  $x + 1 < 9x + 9$  and show the solution on a number line. (04 marks)
- Given matrix  $A = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix}$  and  $I$  is the  $2 \times 2$  identity matrix, show that  $A^{-1} = \frac{1}{2}(A - 7I)$ . (04 marks)

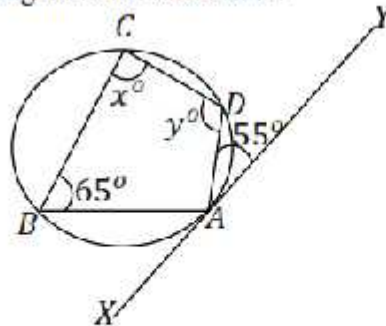
- A pharmacy sells face masks in a variety of sizes. Their sales over a week are recorded in the table below.

Size	Kids		Adults			
	Small	Large	S	M	L	XL
Frequency, $f$	29	4	8	24	15	4

- Write down the mode for this data. (01 mark)
  - Given that the shop is open everyday of the week, calculate the mean number of masks sold per day. (03 marks)
- Express  $x$  in terms of  $p$ ,  $q$  and  $y$  in the expression  $2y = \frac{p}{q + \frac{1}{x}}$ . (04 marks)

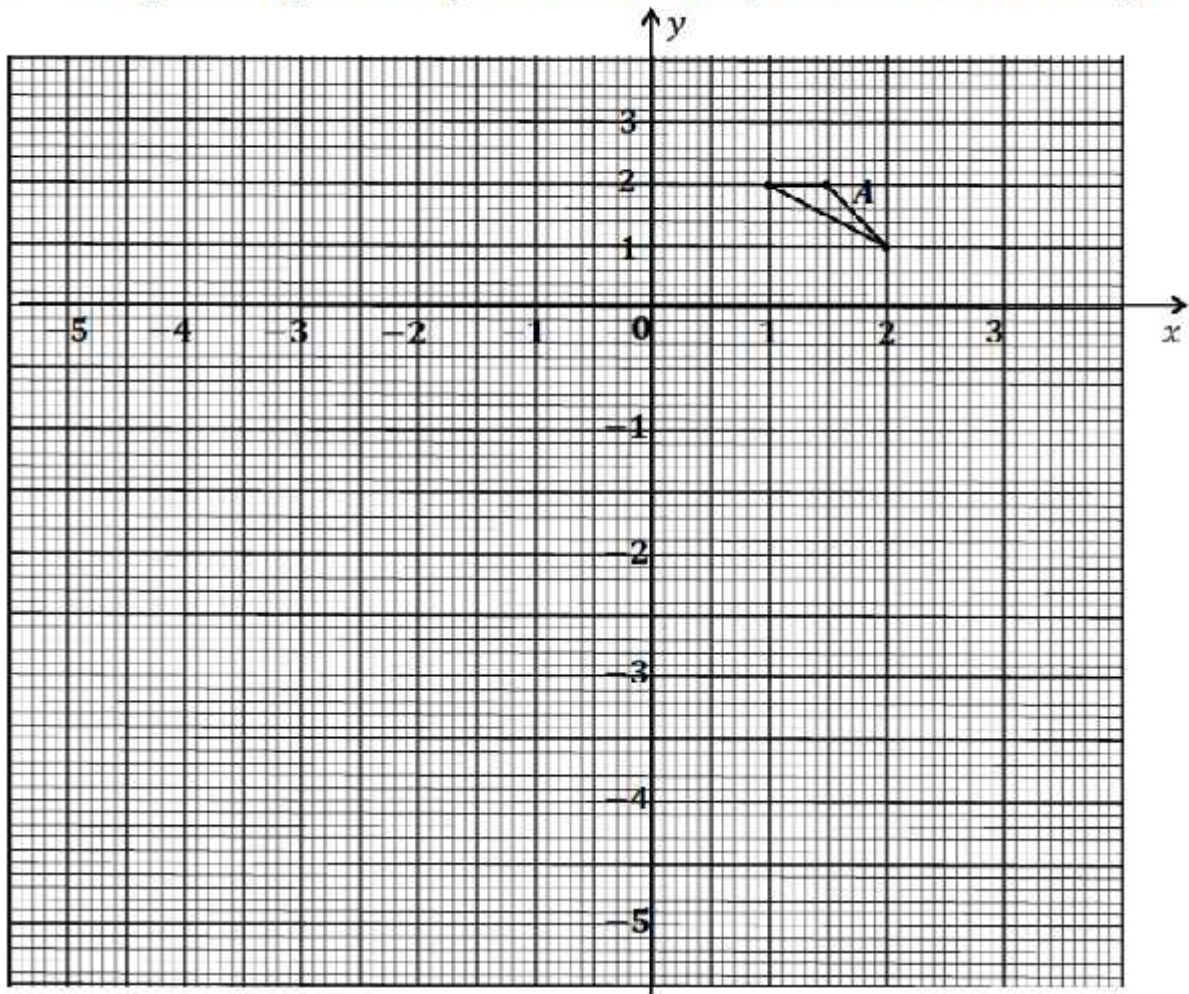
- Given that  $x * y = 1 - xy + x^2 - y$ . Find the value of  $(3 * 2) * -1$ . (04 marks)

- In the diagram below,  $A$ ,  $B$ ,  $C$  and  $D$  are points on the circumference of the circle. The line  $XY$  is a tangent to the circle at  $A$ .



Find the values of  $x$  and  $y$ . (04 marks)

8. Triangle  $A$  undergoes an enlargement transformation by scale factor  $-2$  about the origin.



Plot triangle  $B$ , the image of  $A$  after the enlargement and state the coordinates of the image triangle. (04 marks)

.....  
(Name and Personal Number)



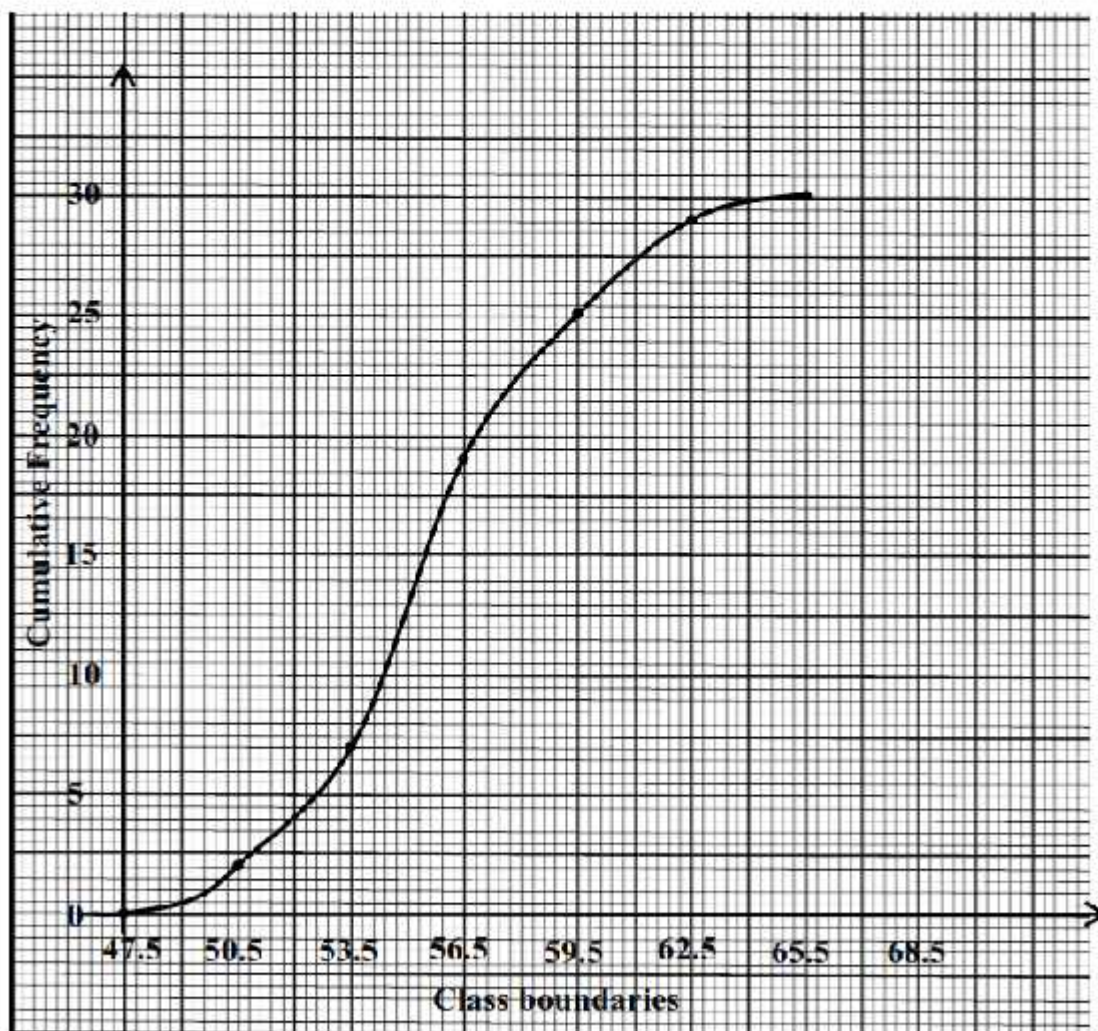
**NB:** *Cut along this line and attach to your answer booklet.  
Remember to write your Name and Personal Number on this sheet.*

9. 16 cards numbered  $\{1, 2, 3, \dots, 16\}$  are put in a box and mixed thoroughly. One person draws a card from the box. Find the probability that the number on the card is divisible by 3 and 2. (04 marks)
10. If  $\tan\theta = \frac{-3}{4}$  and  $\theta$  is reflex, find the value of  $\sin\theta$  (04 marks)

**SECTION B: (60 MARKS)**

*Answer any five questions from this section. All questions carry equal marks.*

11. The cumulative frequency diagram below shows mock results in mathematics examination of Kadama Islamic Secondary School.



Use the graph above to:

- (a) Estimate the median mark. (02 marks)
- (b) Calculate the average mark. (10 marks)

12. (a) Simplify as far as possible. (04 marks)

$$\frac{3x^2y - 27y^3}{3xy - 9y^2}$$

- (b) A garden measuring 15 metres by 20 metres is to have a pedestrian path way installed all around it, increasing the area to  $336m^2$ .
- (i) Given that the width of the path way is  $x$ cm; show that  $2x^2 + 35x = 18$ .
- (ii) Find the possible value of  $x$ . (08 marks)

13. (a) Given that the matrix  $B = \begin{pmatrix} 2 & 1 \\ 1 & 3 \end{pmatrix}$ . Evaluate  $B^2 - 2B$ . (05 marks)

- (b) In a supermarket shs. 8,000 can buy 3 apples and 2 mangoes; sh. 13,000 can buy 4 apples and 5 mangoes.
- (i) Represent this information in matrix form.
- (ii) Find the price of an apple and a mango. (07 marks)

14. (a) Copy and complete the table below.

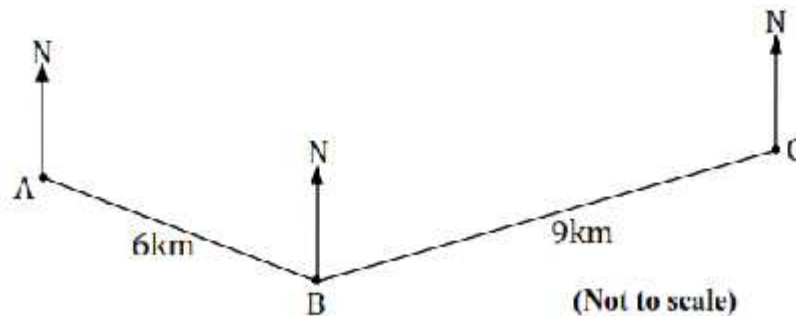
$\theta$	$0^\circ$	$90^\circ$	$180^\circ$	$270^\circ$	$360^\circ$	$450^\circ$	$540^\circ$	$630^\circ$	$720^\circ$
$y = \sin\theta$	0			-1		1			
$y = \cos\theta$	1			0		0			

(03 marks)

- (b) Use your completed table to draw the graphs of  $y = \sin\theta$  and  $y = \cos\theta$  on the same axes. Use a scale of 4cm to represent 1 unit and 2cm to represent  $90^\circ$ . (07 marks)

- (c) Use your graph to solve the equation  $\sin\theta - \cos\theta = 0$  for  $0^\circ \leq \theta \leq 360^\circ$ . (02 marks)

15. A ship sails 6km from A to B on a bearing of  $121^\circ$ . It then sails 9km to C. The size of angle ABC is  $114^\circ$ .



- (a) Copy the diagram into your answer booklet and show all the information on it. (Accurate construction is NOT required) (02 marks)
- (b) What is the bearing of C from B? (03 marks)
- (c) Find the distance AC to the nearest kilometre. (03 marks)
- (d) What is the bearing of A from C? (04 marks)  
Give your answer correct to the nearest degree.

16. (a) On a squared paper, plot the points  $A(2, -1)$ ,  $B(0, -3)$ ,  $C(2, -4)$  and  $D(4, -2)$  and join them to form a quadrilateral  $ABCD$ . What is the name of this quadrilateral? (03 marks)
- (b) The points  $A'(1, 2)$ ,  $B'(3, 0)$ ,  $C'(4, 2)$  and  $D'(2, 4)$  are the images of  $A, B, C$  and  $D$  under a certain transformation  $T_1$ . On the same axes draw quadrilateral  $A'B'C'D'$  and describe transformation  $T_1$  fully. (03 marks)
- (c) The points  $A''(-2, -4)$ ,  $B''(-6, 0)$ ,  $C''(-8, -4)$  and  $D''(-4, -8)$  are the images of  $A', B', C', D'$  under a transformation  $T_2$ . On the same axes draw quadrilateral  $A''B''C''D''$  and describe transformation  $T_2$  fully. (03 marks)
- (d) On the same axes, draw quadrilateral  $A'''B'''C'''D'''$ , the image of  $A''B''C''D''$  under a reflection in the line  $y = 0$ . State the coordinates of  $A'''B'''C'''D'''$ . (03 marks)
17. Aunt Kaduuka sells two types of fresh juice in 250ml cups, Red juice and Yellow juice. Red juice is made from one slice of watermelon, 3 apples and one orange. Yellow juice is made from 3 oranges, 2 apples and a slice of ginger. Aunt Kaduuka has 48 oranges, 42 apples, 10 slices of watermelon and 15 slices of ginger.
- (a) If  $x$  denotes the number of cups of Red juice she makes and  $y$  denotes the number of cups of Yellow juice she makes, write down **six** inequalities representing the above information. (05 marks)
- (b) Represent the inequalities on a graph paper by shading the unwanted regions. (04 marks)  
(Use a scale of 2 cm to represent 5 units on both axes)
- (c) If a cup of Red juice costs sh.1000 and that of Yellow juice costs sh.1200, estimate the maximum profit that can be made by Aunt Kaduuka. (03 marks)